## Shapes of molecules and ions



Student worksheet: CDROM index 33SW


## Topics

Valence shell electron pair repulsion (VSEPR) theory application.

## Level

Very able post-16 students.

## Prior knowledge

Valence shell electron pair repulsion (VSEPR) theory.
(An explanation of the VSEPR theory is given but this activity is best done after some discussion of the theory in class.)
Resolving forces (questions 3 and 4).

## Rationale

This activity draws some extra concepts and mathematical skills into the discussion of molecular shape. A distinction between geometry around the central atom and the shape of the molecule is made. Students are asked to apply the VSEPR theory to some challenging examples, including species with unpaired electrons. Students are introduced to the alternative model of hybridised atomic orbitals.

## Use

This can be used as a follow up to a theory lesson on VSEPR theory for very able students. It can also be used as a differentiated activity for the most able students in a mixed ability group. If the students do not know how to resolve forces, they should leave out questions 3 and 4.

This symbol means those questions are best tackled as a discussion if a group of students is doing this activity.

## Shapes of molecules and ions

An important theory used to explain and predict the shapes of molecules and ions is the Valence Shell Electron Pair Repulsion (VSEPR) theory. This model is based on the idea that the pairs of electrons in the valence, or outer, shell of the central atom repel each other. The species therefore adopts a geometry that minimises the electron pair repulsion. The geometry around the central atom depends on the effective number of electron pairs (double bonds count as one pair because both pairs in a double bond are constrained to point in the same direction). The table below summarises the relationship between the number of electron pairs and geometry.

| Effective number of electron pairs | Geometry | Structure |
| :---: | :---: | :---: |
| 2 | Trigonal planar | Tetrahedral |
| 3 | Trigonal bipyramidal |  |
| 4 | Octahedral <br> 5 | Several - <br> including pentagonal <br> bipyramidal |
| 7 |  |  |
| 6 |  |  |

If the electron pairs are not all the same, some distortion of the geometry can occur. Lone pairs are thought to take up more space around the central atom than double bonds, which in turn take up more space than single bonds. The amount of space taken up by a bonding pair may be affected by the bond polarity.

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## Questions

1. By drawing dot and cross diagrams and carefully counting the electrons or otherwise, suggest the geometry and draw the shapes of the molecules and ions a)-e). Put your answers in a table like the one below:

| Molecule or ion | Effective number <br> of electron pairs in <br> valence shell of <br> central atom | Geometry around <br> central atom | Shape |
| :--- | :--- | :--- | :--- |
|  |  |  |  |

a) $\mathrm{SO}_{2}$ (Hint: it is not linear)
b) $\mathrm{O}_{3}$
c) $\mathrm{IF}_{7}$
d) $\mathrm{SF}_{4}$ (There are five pairs of electrons around the sulfur. You need to think carefully about the position of the lone pair.)
e) $\mathrm{NO}_{3}^{-}$
2. Phosphorus $(\mathrm{V})$ chloride in the solid state is thought to consist of the ions $\mathrm{PCl}_{4}{ }^{+}$and $\mathrm{PCl}_{6}{ }^{-}$. Work out the shape of these ions.
3. By considering each pair of electrons as an equal outward pull on the central nucleus and resolving forces along one of the bonds, show that the bond angle in a symmetric trigonal planar molecule, like $\mathrm{BCl}_{3}$, is $120^{\circ}$.

4. Using a similar method, show that the pure tetrahedral angle is $109.5^{\circ}$.

5. The HCH bond angle in ethene is $117.3^{\circ}$. Calculate how much greater the force of attraction from the double bond is, compared to the single bonds. Comment on your answer.


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## Chemistry for the gifted and talented


6. Phosphorus $(\mathrm{V})$ chloride decomposes on heating to give $\mathrm{PCl}_{3}$ and $\mathrm{Cl}_{2}$. Explain whether it is from the axial or equatorial positions that the chlorines break away.

axial

7. Account for the bond angles in the following molecules:

| Molecule | Bond angle |
| :---: | :---: |
| $\mathrm{NH}_{3}$ | $107^{\circ}$ |
| $\mathrm{NF}_{3}$ | $102^{\circ}$ |
| $\mathrm{CH}_{4}$ | $109.5^{\circ}$ |
| $\mathrm{CH}_{3} \mathrm{Cl}$ | $110.5^{\circ}(\mathrm{HCH})$ |
| $\mathrm{H}_{2} \mathrm{O}$ | $104.5^{\circ}$ |
| $\mathrm{H}_{2} \mathrm{~S}$ | $92.2^{\circ}$ |
| $\mathrm{NO}_{2}$ | $134^{\circ}$ |

An alternative model for explaining the shapes of molecules and ions uses hybrid atomic orbitals (see further reading). The suggested hybridisation for different geometries is shown below.

| Geometry | Linear | Trigonal <br> planar | Tetrahedral | Trigonal <br> bipyramidal | Octahedral |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Hybridisation | sp | $\mathrm{sp}^{2}$ | $\mathrm{sp}^{3}$ | $\mathrm{sp}^{3} \mathrm{~d}$ | $\mathrm{sp}^{3} \mathrm{~d}^{2}$ |

## Further reading

1. To read more about hybridised atomic orbitals, J. Keeler and P. Wothers, Why chemical reactions happen, Oxford: Oxford University Press, 2003 (p82-93).
2. A good website to visit is: www.psigate.ac.uk/newsite/reference/plambeck/chem1/p02201.htm (accessed June 2007).

## Shapes of molecules and ions

1. State the geometry and draw the shapes of the following molecules and ions.

| Question | Molecule <br> or ion | Effective <br> number of <br> electron pairs | Geometry <br> around central <br> atom | Shape |
| :--- | :--- | :--- | :--- | :--- |
| a) | $\mathrm{SO}_{2}$ | 3 (sulfur can <br> expand' its octet) | Trigonal planar | 3 (double bonds <br> count as 1 pair) |
| b) | Trigonal planar |  |  |  |
| c) | $\mathrm{IF}_{7}$ | 7 | Pentagonal <br> bipyramidal | Trigonal <br> bipyramidal <br> (distorted) |
| d) | $\mathrm{SF}_{4}$ | 5 | Trigonal planar |  |

Note: $\operatorname{In} \mathrm{SF}_{4}$ the lone pair could potentially be in an axial position or an equatorial position. The configuration with the lone pair in the equatorial position allows more space for the bulky lone pair, as there are only two other pairs at $90^{\circ}$ to it.


The lone pair takes up more room than bonding pairs of electrons, so the shape is slightly distorted with the bonding electrons pushed away from the lone pair.

The FSF bond angle (for axial fluorines) is $173.1^{\circ}$.

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$\mathrm{SF}_{4}$, $\mathrm{SO}_{2}$ and $\mathrm{IF}_{7}$ are all examples of where the central atom has 'expanded its octet' - ie contains more than eight electrons in its valence shell. This is easier in the third period of the Periodic Table than in the first or second periods because of the availability of $d$ atomic orbitals..

The nitrate ion is thought to have a conjugated structure (as shown in the second structure), in a similar way to carboxylate ions.
2. Phosphorus(V) chloride in the solid state is thought to consist of the ions $\mathrm{PCl}_{4}{ }^{+}$and $\mathrm{PCl}_{6}{ }^{-}$. Work out the shape of these ions.

3. By considering each pair of electrons as an outward pull on the central nucleus and resolving forces along one of the bonds, show that the bond angle in a symmetrical trigonal planar molecule like $\mathrm{BCl}_{3}$ is $120^{\circ}$.

Each arrow represents a force of y . Resolving forces in the horizontal direction, $2 y \cos \theta=y$ because the forces on the nucleus must be balanced, $\cos \theta=1 / 2$ therefore $\theta=60^{\circ}$.
$180^{\circ}-60^{\circ}=120^{\circ}$, or bond angle $=2 \theta=120^{\circ}$.

4. Using a similar method, show that the pure tetrahedral angle is $109.5^{\circ}$.

The method is the same, but this time there are three arrows pointing to the left so $3 y \cos \theta=y$ $\cos \theta=1 / 3$ therefore $\theta=70.5^{\circ}$

Thus bond angles $180^{\circ}-70.5^{\circ}=109.5^{\circ}$.
5. The HCH bond angle in ethene is $117.3^{\circ}$. Calculate how much greater the force of attraction from the double bond is, compared to the single bonds. Comment on your answer.

Let $d$ be the pull from the double bond and let $s$ be the pull from the single bond. Resolving forces along the double bond gives:

$$
d=2 s \cos 58.65^{\circ}
$$

$d=1.04 \mathrm{~s}$.
This is surprisingly small, given that there are four electrons in the double bond compared with only two in the single bond. The explanation for the surprisingly small attraction along the axis of the double bond must be that, because the electron density of the $\pi$ electrons is largely above and below the plane of the molecule, most of the attraction of the $\pi$ electrons is perpendicular to the attraction of the $\sigma$ electrons.
6. Phosphorus(V) chloride decomposes on heating to give $\mathrm{PCl}_{3}$ and $\mathrm{Cl}_{2}$. Explain whether it is from the axial or equatorial positions that the chlorines break away.

Chlorines break away from the axial positions since these are more crowded, with three neighbours at $90^{\circ}$ rather then two neighbours at $90^{\circ}$ and two at $120^{\circ}$ for the equatorial chlorines.
7. Account for the bond angles in the following molecules:

| Molecule | Bond angle |
| :---: | :---: |
| $\mathrm{NH}_{3}$ | $107^{\circ}$ |
| $\mathrm{NF}_{3}$ | $102^{\circ}$ |
| $\mathrm{CH}_{4}$ | $109.5^{\circ}$ |
| $\mathrm{CH}_{3} \mathrm{Cl}$ | $110.5^{\circ}(\mathrm{HCH})$ |
| $\mathrm{H}_{2} \mathrm{O}$ | $104.5^{\circ}$ |
| $\mathrm{H}_{2} \mathrm{~S}$ | $92.2^{\circ}$ |
| $\mathrm{NO}_{2}$ | $134^{\circ}$ |

The $\mathrm{NH}_{3}$ bond angle is $107^{\circ}$. This is distorted from the pure tetrahedral angle by the lone pair taking up more space than the single bonds.

The $\mathrm{NF}_{3}$ bond angle is $102^{\circ}$. There is more distortion than for $\mathrm{NH}_{3}$ because the single bonds are taking up less room, close to the nitrogen. Fluorine is more electronegative than hydrogen and the electron density in the N-F bond is skewed towards the fluorine.

The $\mathrm{CH}_{4}$ bond angle is $109.5^{\circ}$. This is the undistorted tetrahedral angle.

The $(\mathrm{HCH})$ bond angle in $\mathrm{CH}_{3} \mathrm{Cl}$ is $110.5^{\circ}$. The HCH bond angle is wider than in $\mathrm{CH}_{4}$ which suggests that the $\mathrm{C}-\mathrm{Cl}$ single bond takes up less space close to the carbon. This is due to the $\mathrm{C}-\mathrm{Cl}$ bonds polarity with $\delta^{-}$on the chlorine, chlorine being more electronegative than carbon (and hydrogen). The $\mathrm{C}-\mathrm{H}$ bond has more electron density around the carbon because the carbon is $\delta^{-}$, carbon being more electronegative than hydrogen.

The $\mathrm{H}_{2} \mathrm{O}$ bond angle is $104.5^{\circ}$. There is greater distortion than in $\mathrm{NH}_{3}$ because there are two lone pairs on the oxygen.

The $\mathrm{H}_{2} \mathrm{~S}$ bond angle is $92.2^{\circ}$. There is a surprisingly large difference between this and the bond angle in $\mathrm{H}_{2} \mathrm{O}$. Sulfur is less electronegative than oxygen, so the $\mathrm{S}-\mathrm{H}$ bond takes up less space around the central atom than the $\mathrm{O}-\mathrm{H}$ bond. In terms of hybridisation, the reduced bond angle in $\mathrm{H}_{2} \mathrm{~S}$ implies the bonds that are formed are much closer to p atomic orbitals, rather than $\mathrm{sp}^{3}$ hybrid atomic orbitals. A reason for this might be weaker bonds, therefore less return on the investment in energy to hybridise the atomic orbitals.

The $\mathrm{NO}_{2}$ bond angle is $134^{\circ}$. This is a perhaps a surprising value. The first step towards explaining this is to propose a structure for $\mathrm{NO}_{2}$ that is consistent with this bond angle.


Around the nitrogen there is a double bond, a single bond and an unpaired electron (remember that $\mathrm{NO}_{2}$ dimerises to form $\mathrm{N}_{2} \mathrm{O}_{4}$ ). The geometry is trigonal planar but the unpaired electron repels the bonding pairs less than a pair of electrons so the bond angle is greater than $120^{\circ}$.

For more discussion on $\mathrm{NO}_{2}$ visit:
http://dbhs.wvusd.k12.ca.us/webdocs/VSEPR/Odd-Electron-Molecules.html
(accessed May 2007).


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